| Progression in the Teaching of Calculations |  |  |  |
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| SUBTRACT IT! |  |  |  |
| Objective/ strategy | Concrete - build it/ use it! | Pictorial - draw it! | Abstract - solve it! |
| Taking away ones | Use real life physical objects and take away an amount from a given group. How many are left? $6-2=4$ | Cross out drawn objects to show what has been taken away. <br> $5-2=3$ | $\begin{aligned} & 4=6-2 \\ & 18-3=15 \\ & 8-2=6 \end{aligned}$ |
| Counting backwards | Use counters and move away counters while counting backwards. <br> Use cubes while counting backwards | Count back on a number track. <br> Count backwards on a number track starting from the greatest value, showing the jumps of partitioned tens and ones. | $13-4=9$ <br> Put 13 in your head and count back 4. Use your fingers and number bonds to help when you cross the tens. |


|  | to take away an amount. <br> Find the greatest number in the calculation and start with it. Then, count backwards with the subtrahend from the minuend. |  |  |
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| Find the difference | Compare amounts and objects to find the difference. Use cubes to make bars or towers to see the difference between numbers. <br> Use simple comparative bar models and physical objects to spot the difference. | Count on to find the difference. 11-6 $=5$. <br> Use comparison bar models to show the difference between values. <br> Lisa is 13 years oid. Her sister is 22 years old Find the difference in age between them. <br> Draw bars to show the difference. | Hannah has 23 pencils and Helen has 15 pencils. What is the difference between the number of pencils that the girls have? |


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| Part-whole model for subtraction | Link to addition and use the part whole model to show the inverse. <br> If 10 is the whole and 5 is the part, what is the other part? 10-5 = ? or 10 - ? = 5 | Use pictorial representations to show the part-whole model with objects and drawings. | Write the equations to match the part whole models. $\begin{aligned} & 10-5=5 \\ & 5=10-5 \end{aligned}$ |
| Make 10 | Make 14 on the tens frame then take away the four fist so you have 10. Then takeaway one more so you have taken away 5 altogether. You are left with 9 . | $13-7=6$ <br> Start at 13 . Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. | $16-8=?$ <br> How much do we need to take away until we reach 10? Then, take away the rest. |


|  | $\begin{aligned} & 14-5= \\ & 14-4=10 \\ & 10-1=9 \end{aligned}$ | Draw the number line and count the jumps back. Create one jump to get to 10. Then take away the rest. |  |
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| Column method without regrouping expanded into compact method | $75-42=$ <br> Use Dienes to make the greatest number then take the smaller number away. Show how your partition numbers to subtract in their place value columns. | Draw the Dienes or place value counters alongside the written calculation to help to show working. | Layout the column method as shown below. Align the digits in the correct place value columns. $\begin{gathered} 47-24=23 \\ -20+7 \\ -20+3 \\ \hline \end{gathered}$ |


|  | $\begin{array}{ll\|l\|l\|} \hline 36-14=22 \\ \frac{T}{9} & 4 & \frac{T}{30} & 4 \\ \hline 8 & 3 & -\frac{10}{20} & 4 \\ \hline 8 & & 20 & 2 \end{array}$ |  |  |
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| Column method with regrouping expanded into compact method | Make the greatest number with the Dienes or place value counters. Start with the ones, can I take 8 ones away from 4 ones in this method? I need to exchange one of my tens for ten ones and regroup it in the ones column. <br> Use a ten and regroup it for ten ones. Then take 8 ones away from 14 ones. <br> Now you have 2 tens left. We need to regroup 1 hundred for 10 tens so that we can take 8 tens away from 12 | Draw the counters onto a place value grid and show what has been taken away by crossing the counters out as well as clearly showing the regrouping made. | Start by using the expanded column method where the parts of the number are shown fully (and not just as digits). <br> Then, align the digits and take away in the compact column method. <br> Then, take away decimal numbers with the same amount of decimal |


|  | tens. Then, we can complete the calculation. |  | places. <br> Finally, move on to subtracting decimals with different decimal places. $\begin{array}{rrrrr}  & 5 & 12 & 1 \\ 2 & 6 & 3 & & 0 \\ & 2 & 6 & & 5 \\ \hline 2 & 3 & 6 & . & 5 \end{array}$ |
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| Subtracting fractions | Use real life objects to show fractions, such as $5 / 5$ of the cake $=1$ whole of the cake. <br> If I have $5 / 5$ and I take away $2 / 5$, how many fifths do I have left? | Draw bar models to represent an amount. $5 / 5-1 / 5=4 / 5$ <br> Cross out the fraction that you need to take away when subtracting fractions with the same denominator. <br> Then, find equivalent fractions by drawing bars and finding the equal parts below it. | Encourage children to spot the relationships between equivalent fractions in order to find a common denominator. |


|  |  |  | $\begin{aligned} & \frac{3}{4}-\frac{1}{8}= \\ & \frac{3 \times 2}{4 \times 2}-\frac{1}{8} \\ & \frac{6}{8}-\frac{1}{8}=\frac{5}{8} \end{aligned}$ |
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